

CHEMISTRY STUDY MATERIALS FOR CLASS 9

(NCERT based Revision of Atoms and molecules)

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NUMERICAL PROBLEMS BASED ON MOLE CONCEPT

Question 22. Find the charge of 1 g-ion of N^{3-} in *Coulombs*.

Solution22. Charge on 1 N^{3-} ion = $3 e^{-} = 3 \times 1.602 \times 10^{-19}$ *Coulombs*

$$\begin{aligned}\text{Charge on 1 g-ion of } N^{3-} &= 3 \times 1.602 \times 10^{-19} \times 6.022 \times 10^{23} \text{ Coulombs} \\ &= \mathbf{2.894 \times 10^5 \text{ Coulombs.}}\end{aligned}$$

Question 23. Find the charge of 27 g of Al^{3+} ions in *coulombs*.

Solution23. Atomic mass of Al = 27

$$\text{No. of moles Al} = 27/27$$

$$= 1 \text{ mole}$$

Charge on 1 Al^{3+} ion = $3 e$

$$= 3 \times 1.602 \times 10^{-19} \text{ Coulombs}$$

$$\begin{aligned}\text{Charge on 1 mole } Al^{3+} \text{ ions} &= 3 \times 1.602 \times 10^{-19} \times 6.022 \times 10^{23} \text{ Coulombs} \\ &= \mathbf{2.894 \times 10^5 \text{ Coulombs.}}\end{aligned}$$

Question 24. Equal masses of oxygen, hydrogen and methane are taken in a container in identical conditions. Find the ratio of the volumes of the gases.

Solution24. Let X g of each gas is taken. Then,

$$\text{Mole ratio} = O_2 : H_2 : CH_4$$

$$= X/32 : X/2 : X/16$$

$$= 1:16:2.$$

$$= \text{Volume ratio}$$

[∵ Avogadro's Principle – the molar ratios are also volume ratios for gases]

$$\therefore O_2 : H_2 : CH_4 = \mathbf{1 : 16 : 2.}$$

Question 25. If the components of the air are N_2 , 78%; O_2 , 21%; Ar, 0.9% and CO_2 , 0.1% by volume, what would be the molecular mass of air?

Solution 25. The molar ratios are also volume ratios for gases (Avogadro's principle)

$$\begin{aligned}\text{Molecular mass of air} &= \frac{(78 \times 28 + 21 \times 32 + 0.9 \times 40 + 0.1 \times 44)}{(78 + 21 + 0.9 + 0.1)} \\ &= \mathbf{28.964}.\end{aligned}$$

Question 26. The atomic masses of two elements (A and B) are 20 and 40 respectively.

x g of A contains y atoms, how many atoms are present in 2x g of B?

Solution 26. No. of mole of A = $x/20$

No. of atoms of A = $(x/20) \times N$ [N is Avogadro constant]

$$\therefore y = x \times N/20$$

$$\Rightarrow x = 20y/N$$

Now,

No. of mole of B = $2x/40$

No. of atoms of B = $(2x/40) \times N$

$$= 2N/40 \times 20y/N$$

$$= \mathbf{y}.$$

Question 27. Oxygen is present in a 1-liter flask at a pressure of 7.6×10^{-10} mm of Hg at $0^\circ C$. Calculate the number of oxygen molecules in the flask.

Solution 27. Pressure = 7.6×10^{-10} mm Hg = $7.6 \times 10^{-10}/760$ [1 atm = 760 mm Hg]
 $= 10^{-12}$ atm

Volume = 1 liter

Temperature = $0^\circ C = 273$ K

We know $pV = nRT \Rightarrow n = pV/RT$

$$n = (10^{-12} \times 1)/(0.0821 \times 273)$$

$$= 0.44 \times 10^{-13}$$

No. of molecules = no. of moles \times Avogadro constant

$$= 0.44 \times 10^{-13} \times 6.022 \times 10^{23}$$

$$= \mathbf{2.65 \times 10^{10}}.$$

Question 28. Calculate approximately the diameter of an atom of mercury, assuming that each atom is occupying a cube of **edge length equal to the diameter** of the mercury atom. The density of mercury is 13.6 g/cc.

Solution 28. Suppose the side of cube = x cm = diameter of mercury atom

$$\therefore \text{Volume of 1 Hg atom} = x^3 \text{ and}$$

$$\begin{aligned} \text{Mass of 1 Hg atom} &= \text{density} \times \text{volume} \\ &= 13.6 \times x^3 \end{aligned}$$

$$\begin{aligned} \text{Mass of 1 Hg atom} &= \text{Atomic mass} / \text{Avogadro constant} \\ &= 200 / 6.022 \times 10^{23} \end{aligned}$$

$$13.6 \times x^3 = 200 / 6.022 \times 10^{23}$$

$$\Rightarrow x^3 = 200 / (13.6 \times 6.022 \times 10^{23}) = 2.44 \times 10^{-23}$$

$$\Rightarrow x = (2.44 \times 10^{-23})^{1/3} = \mathbf{2.9 \times 10^{-8} \text{ cm.}}$$

Question 29. The density of a particular crystal of LiF is 2.65 g/cc. X-ray analysis shows that Li^+ and F^- ions are arranged in a cubic array at a spacing of 2.01 Å. From these data calculate the apparent Avogadro constant.

$$[\text{Li} = 6.639\text{u}, \text{F} = 18.998\text{u} (1 \text{ \AA} = 10^{-8} \text{ cm})]$$

Solution 29. Avogadro constant = No. of LiF molecules present in 1 mole

$$(6.639 + 18.998 = \mathbf{25.937\text{g}})$$

$$\begin{aligned} \text{Volume of 1 mole LiF arranged in cube} &= \text{mass} / \text{density} \\ &= 25.937 / 2.65 = 9.78 \text{ cc.} \end{aligned}$$

$$\text{Length of edge of the cube} = (9.78)^{1/3} = 2.138 \text{ cm}$$

$$\begin{aligned} \text{No. of ions present in one edge of the cube} &= 2.138 / 2.01 \times 10^{-8} \\ &= 1.063 \times 10^8 \end{aligned}$$

$$\begin{aligned} \text{No. of ions } (\text{Li}^+ \text{ and } \text{F}^-) \text{ present in the cube} &= (1.063 \times 10^8)^3 \\ &= 1.201 \times 10^{24} \end{aligned}$$

No. of LiF molecule per mole = Avogadro constant

$$\begin{aligned} &= 1.201 \times 10^{24} / 2 \\ &= \mathbf{6.01 \times 10^{23}.} \end{aligned}$$
